



# Kinetic Study and Modeling of Nigerian Sub Bituminous Coal Char Using the Random Pore Technique

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## Authors' contributions

*This work was carried out in collaboration between both authors. Both authors read and approved the final manuscript.*

## Article Information

DOI: 10.9734/JERR/2023/v25i9978

## Open Peer Review History:

This journal follows the Advanced Open Peer Review policy. Identity of the Reviewers, Editor(s) and additional Reviewers, peer review comments, different versions of the manuscript, comments of the editors, etc are available here: <https://www.sdiarticle5.com/review-history/105176>

**Original Research Article**

**Received: 01/07/2023**

**Accepted: 03/09/2023**

**Published: 25/09/2023**

## ABSTRACT

In order to augment the short supply of energy for industrial purposes, the kinetics of carbon-dioxide gasification of two Nigerian sub bituminous coal chars was studied in this work using a thermogravimetric analyser (TGA). This paper reports the findings on gasification of typical Enugu (Udi) and Kogi (Okaba) coal of Nigeria in carbon dioxide medium at atmospheric pressure. Proximate and ultimate analysis was performed on the coal samples based on their origin to determine their properties and values. Result shows that Udi coal has a higher heating value as compared to Okaba coal. The effect of the temperature of gasification ranging from 900°C to 1000°C at different concentration of carbon dioxide of 100%, 70% and 40% at atmospheric pressure was studied. The gasification process of coal involves pyrolysis and char gasification. It was found that the reactivity of char gasification increased with the increase of pyrolysis heating rate, which demonstrates the effect of temperature on gasification. A random pore model approach with a novel kinetic scheme was used to describe the behaviour of the coal char. The simulated predictive model result was compared with the observed experimental result, which were in good agreement. Based on the obtained result, it was observed that the rate of carbon conversion increases with increase in concentration of carbon dioxide over time, and vice versa. The activation

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energy for the coal samples vary depending on their origin and were found to be 97.58kJ/mol and 103kJ/mol for Kogi coal and Enugu coal respectively. Products of coal gasification will serve as a promising fuel alternative.

*Keywords: Coal; kinetics; char gasification; random pore model; Thermogravimetric Analyser (TGA) and carbon-dioxide.*

## 1. INTRODUCTION

Coal is the largest most abundant fossil fuel resources in the world and has played and will continue to play an essential role in supplying the energy needed for economic growth. The increasing demand for conventional fuel production. As a result, a cleaner and more efficient coal technology has gained more attention [1]. Product from coal gasification can be considered as a promising fuel for Nigeria's future growth, since there are large coal reserves in the country, which total over 2billion tons. These coal reserves are situated in places like Enugu, Okaba, Newi, Nasarawa, Benue, and Gombe of Nigeria and there are still more reserves that have not been discovered. Different technologies like Integrated Gasification Combined Cycle (IGCC), Pressurized Fluidized Bed Combustion (PFBC) have been and are being developed to overcome the many environmental problem of air and water pollution associated with the use of coal as a fuel [2].

The design of a gasifier depends on the kinetic parameter for the gasification of char in addition to the pyrolysis kinetic parameters. Many models have been suggested over the years, moving from the simplest one step to more complicated random pore, grain model. In most model of coal char gasification, particles are normally assumed to be spherical, uniformly porous solids but in realities this is not the case as char from the same coal can exhibit different range of morphologies and porosities [2].The choice of model solution depends on the conditions of the structure of the solid phase and the transport and reaction rate. The complexity of the model depend mainly on the type of heterogeneous reaction and simplifying assumptions [3]. Also the physical properties of the coal char, such as pore structure and surface area varies with conversion, depending upon gasification conditions [4].

The overall reactivity of coal char depends on the accessibility of the internal surface area to the gaseous reactant, which is determined by the porous structure of the coal particles [5,6].

In a bid to augment for the short supply of energy needed for industrial purposes in Nigeria, the study of the reactivity and kinetics of char gasification at different concentrations of CO<sub>2</sub> and at three different temperatures was researched into. A predictive random pore model was tested and presented. Char was prepared from Okaba and Udi subbituminous coals.

## 2. MATERIALS AND METHODS

### 2.1 Coal Sample

Okaba and Udi Subbituminous coal samples were crushed using mortar and pestle and then sieved to a size fraction (75 - 150 $\mu$ m). The coal particles were then dried in oven at 70°C for 2 h.

### 2.2 Pyrolysis of Coal

The subbituminous coal sample was pyrolyzed using a furnace (MODEL-EL195 FISHER UK) at the temperature of 800 °C with a heating rate of 10 °C/min and 30 °C/min in nitrogen atmosphere. The proximate and ultimate analysis for the coal char was carried out.

### 2.3 Coal Char Gasification in a Thermogravimetric Analyser (TGA)

The Thermo Gravimetric Analysis (TGA) facility at the National Research Institute for Chemical Technology (NARICT) Kaduna, Nigeria was incorporated to obtain the gasification rate. The TGA was used to monitor the weight change by isothermal analysis. Char samples from Okaba coal and Udi coal were gasified in a Thermogravimetric Analyser (TGA) in the temperature range from 900°C to 1000°C. The computer controlled TGA constantly measures the weight of materials as a function of time and temperatures. See Fig. 1. for schematic diagram of TGA.

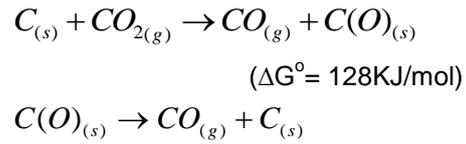
Gasification of coal char with different carbon dioxide concentration (100%, 70% and 40% CO<sub>2</sub>) was performed at 900 °C – 1000 °C at a

heating rate of 5°C/min for different carbon dioxide concentration. Readings for the mass change of the char was taken at every 10mins interval. 20 mLmin<sup>-1</sup> Nitrogen was used to vary the concentration of carbon dioxide. For each run 20 mg of char was weighed and placed onto the crucible, placed in the centre of the reaction chamber of the TGA. The volumetric flow rate of the gaseous phase was ranged between 0.2 to 0.6 L/h.

The capability X-ray diffraction method (XRD) equipped with a diffractometer was used to analyze the crystalline properties of samples. The X-ray patterns were recorded using Cu K $\alpha$  radiation. The power supply was 55kV and 50mA. The peaks were obtained at 2 $\theta$ , scan speed at 0.4 /step increment of 0.003 degree. Peaks of structures were compared with those of the reference materials. The XRD analysis was carried out at the National Steel and Raw Material Research Institute, Kaduna.

### 2.4 Theory

The mathematical model of coal char gasification is presented. To perform modeling, it is essential to know the kinetics of the reaction taking place during gasification [7,8]. The generally accepted mechanism of the reaction between carbon dioxide and coal char, involving free carbon active site follows the form below: [9,10].



The reaction rate is equal to the rate of decomposition of C(O)<sub>s</sub> intermediate.

The rate  $r_c$  of heterogenous gas/solid reaction for coal char conversion at a given level of carbon conversion and at constant reaction gas pressure can be expressed as Equation 1: [4,11]

$$r_c = \frac{\partial c_c}{\partial t} = \frac{1}{1 - x_s} \frac{\partial x_s}{\partial t} = KC_c C_{c_{o_2}} \quad (1)$$

In complementary studies, Hurt & Haynes, [12] found that the amount of stable complex remaining on the surface of the char after partial gasification and subsequent removal at higher temperature by temperature programmed desorption on the char, also increased monotonically with conversion. This is due to the gas diffusion especially at high temperatures. Distinguishing intrinsic and effective reaction rate is indeed particularly difficult, and this led to the usage of apparent reaction rate as the char gasification reactivity index. The apparent reaction rates (dX/dt) are obtained indirectly from the derivative of carbon conversion (X) versus reaction time (t).

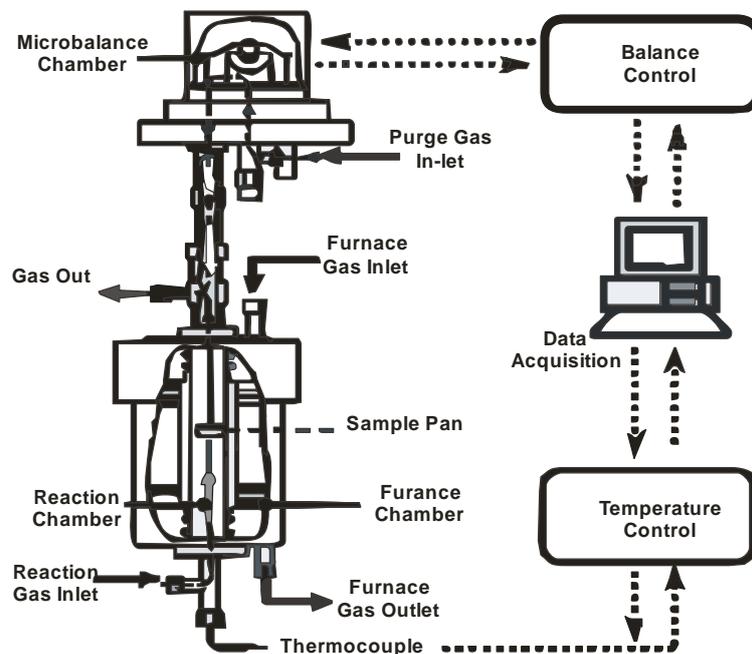


Fig. 1. Schematic diagram of the TGA.

The rate of a heterogeneous gas/solid reaction at a given level of conversion  $X_s$  and at constant gas pressure can be expressed according to Equation 2 [13,14].

$$Rate = \frac{1}{1 - X_s} \frac{\partial x_s}{\partial t} = KC_{(s)} \quad (2)$$

Char conversion  $X$ , (dry, ash free.) is expressed as Equation 3 :

$$X = 1 - \frac{W}{W_o} \quad (3)$$

Where  $W$  and  $W_o$  are the weights of the remaining solid at time  $t$  and initial weight of char at  $t= 0$ , respectively [15,16].

In this research work, the random pore model (RPM) is applied to determine the kinetics of the coal char formation, since it considers the physical structural change during the gasification reaction. The model is applied together with a Temperature Programmed Reaction (TPR) of char gasification reaction carbon dioxide medium. TPR is a method wherein the weight loss is measured during the heating of a solid sample in a reactive gas medium to a desired pre-determined temperature at constant heating rate [3,17]. The basic idea of random model pore is that gasification follows different steps: adsorption of the reacting gas on the surface, reaction and diffusion of adsorbed species and finally release of carbon containing gases. The following assumptions are present in the model; char is described as a pure carbon matrix, ashes if present are considered as inert, char mass loss during gasification is due to desorption of carbon containing gases [17]. The carbon particle is assumed to be spherical and relatively equal. The reaction gas concentration is uniform throughout the carbon particle. The RPM also assumes that the reaction is initiated on the surfaces of the pores in chars. As further reaction occurs, a layer of gas product is formed around each pore which separates the growing reaction surface of the carbon from the gas reactant within the pores. Reactant diffuses through the product layer to reaction surface where chemical change occurs. Although the RPM considers the physical structural changes during the gasification reaction, it does not consider the random pore overlapping and neglects all diffusion resistances in the char reaction [17].

The derived random model equation is obtained as Equation 4:

$$\frac{dx_c}{dt} = k_o e^{-(E_a/RT)} C_{co_2} (1 - x_c) S_{gc} \sqrt{1 - \psi \ln(1 - x_c)} \quad (4)$$

Where  $\psi$  = Structural parameter as defined by Equation 5:

$$\psi = \frac{4\pi l_o}{\rho_c S_o^2} \quad (5)$$

The integral version of the random pore model follows the form given in Equation 6:

$$x_c = 1 - \text{Exp} \left( \frac{1}{\psi} - \frac{\psi k_o^2 s_{gc}^2 (C_{co_2})^2 e^{-2E_a/RT} t}{4} \right) \quad (6)$$

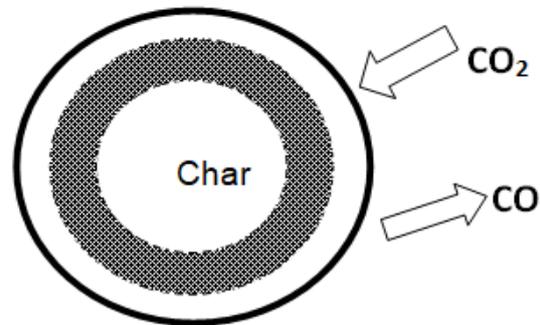


Fig. 2. Schematic diagram of char gasification

### 3. RESULTS AND DISCUSSION

Normally the char gasification of coal conversion is the rate determining step of the overall process. Experiments were performed to determine the rate of  $CO_2$  gasification of the coal char at temperatures ranging from 1173K to 1273K, with data of conversion rate versus reaction time. A gas-solid reaction kinetic model has been developed and applied to the Char- $CO_2$  systems. The model prediction compares favourably to the measured data.

Fig. 3. shows raw data of TGA results for coal char gasification. Weight loss measurements were made under isothermal and transient conditions in the TGA at atmospheric pressure.

Using the char sample produced from the sub-bituminous coal, test at various temperature and gas concentrations indicated that 1000K was the highest temperature at which there were negligible mass transport effects during char gasification of 75 - 150 $\mu$ m diameter particles.

At higher temperatures, the overall mass loss rates were found to depend on the amount of material placed in the balance pan of the TGA, indicative of mass transfer limitation.

Based on the result obtained, which shows that the carbon conversion versus gasification time takes an S-Shaped form. That is to say the reaction rate initially increases during the gasification reaction.

### 3.1 The Micro-Structural Parameter

The XRD in Fig. 4 shows the XRD pattern for Udi coal char sample pyrolyzed at 800 °C and 1000 °C. The main peaks of crystal structure detected in XRD consist of quartz (SiO<sub>2</sub>), calcium oxide (CaO) and calcium sulfide (CaS). Peaks of crystal structures were obtained by comparing with structures of reference materials available in the XRD coal library and based on the elements in the sub-bituminous coal. From these result of the XRD, it can be observed that most of crystal structures peaks of char sample from pyrolysis at 1000 °C are higher than those of char sample from pyrolysis at 800 °C, except for calcium oxide. It is well recognized that CaO is a primary specie which act as a catalyst in the gasification process, on the basis of simplicity and efficiency. Thus, low gasification reactivity of char samples is probably due to the formation of inert crystal

structures and the consumption of CaO at higher pyrolysis temperature [18].

Proximate analysis is the most often used technique for characterizing coal samples in connection with their utilization and usefulness. The proximate analysis on the coal samples in Table 1 shows that Udi coal has a higher risk of spontaneous combustion or ignition than Okaba coal because it contains more volatile matter. The ultimate analysis indicates the various elemental chemical constituents as shown in Table 1. The analysis indicates that Udi coal has a slightly greater carbon content and calorific (heating value) than Okaba coal. This difference in value is 2.1% and 2,430KJ/kg respectively. Nonetheless, both coal samples are suitable for fuel.

### 3.2 Comparism of Experimental Result with Model Result at Different Temperatures and Carbon Dioxide Concentrations

From the trend of results, it was observed that the complete conversion of char in carbon dioxide is attained with less time at high CO<sub>2</sub> concentration. But as the concentration of CO<sub>2</sub> is reduced, the rate of conversion is reduced, thereby increasing the time required for conversion.

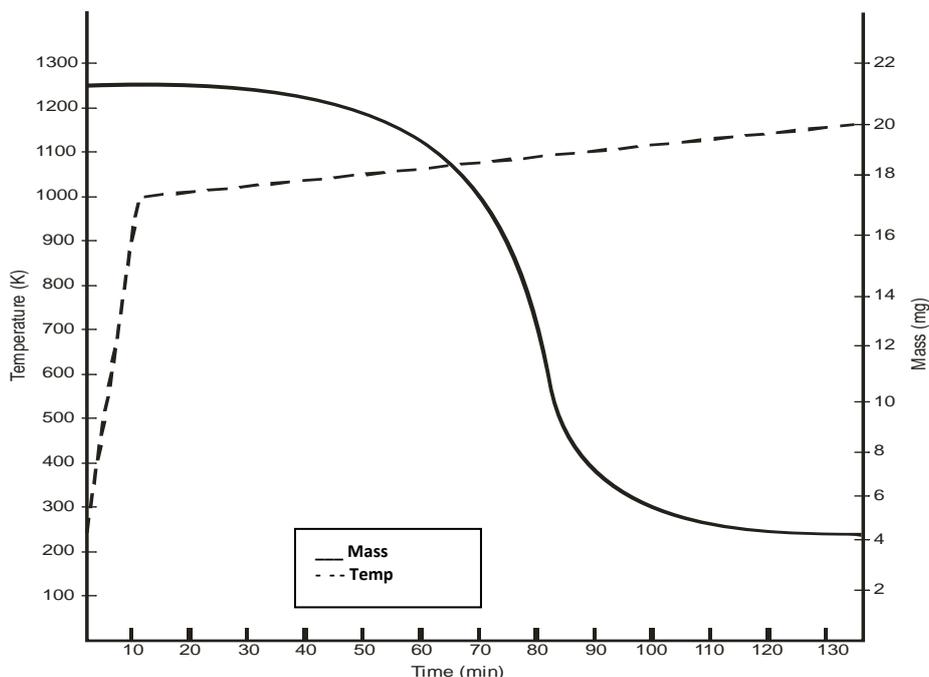
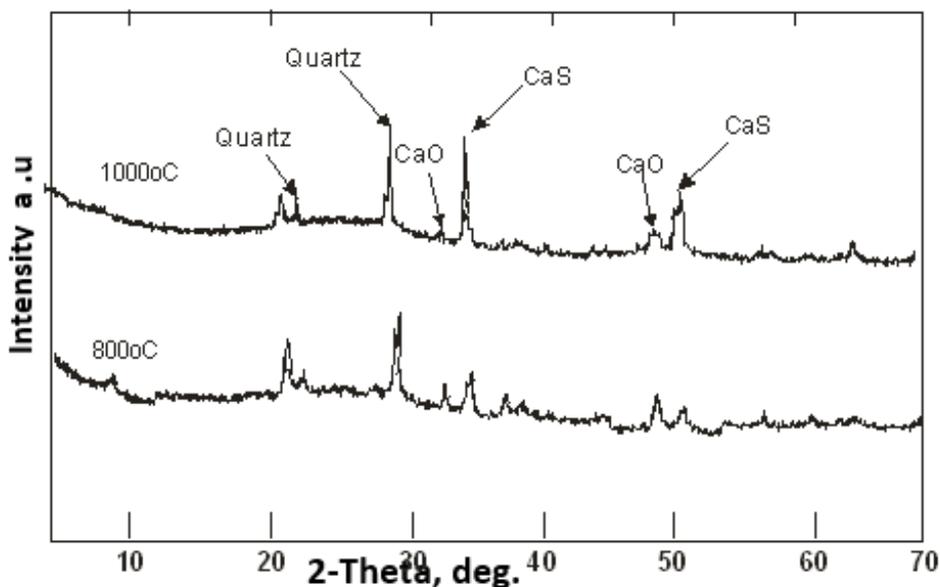


Fig. 3. Non isothermal combustion and gasification of coal char in CO<sub>2</sub> at 5°C/min

**Table 1. Proximate and Ultimate analysis for the coal samples**

	Enugu (Udi) Coal	Kogi (Okaba) Coal
1	Average particle Size	75- 150 µm diameter. 75-150 µm diameter.
2.	PROXIMATE ANALYSIS	
	Moisture %	4.8 4.6
	Ash%	20.4 22.8
	Volatile matter %	40.8 35.9
	Fixed carbon%	41.3 36.8
3	ULTIMATE ANALYSIS	
	Total sulphur %	0.4 0.9
	Carbon%	63.5 61.4
	Hydrogen%	2.59 1.7
	Nitrogen%	1.6 1.3
	Oxygen%	8.3 11.5
	Calorific Value kJ/kg	24,780 22,350



**Fig. 4. X-ray Diffraction pattern for Udi coal char pyrolyzed at two different temperatures (1000°C and 800°C) respectively**

From the graphical result of thermogram, it can be observed that the model does predict the rate of coal char gasification in a carbon-dioxide atmosphere.

The result for that of Okaba coal char gasification, show a similar trend with Udi coal char. The time taken for completion conversion is slightly longer than that of Udi Coal char.

Fig. 5 to Fig. 10 (Udi and Okaba coal) shows the steady rate variation with conversion (time) for sub-bituminous coal char gasified at different CO<sub>2</sub> concentration at atmospheric pressure at 1000 °C, 950 °C and 900 °C respectively. A

monotonically increasing specific gasification rate is observed in all cases.

The thermogram for simulated model and the experimental results reveal that the rate of conversion of coal char decreases with decreasing carbon dioxide concentration. As the concentration of carbon dioxide increases, the time for complete conversion decreases.

From all the thermogram in Equation 10 it is observed that at higher level of conversion, a steep rise in the rate of conversion over time is observed. Also, it was observed that increase in concentration of carbon dioxide leads to increase in the conversion.

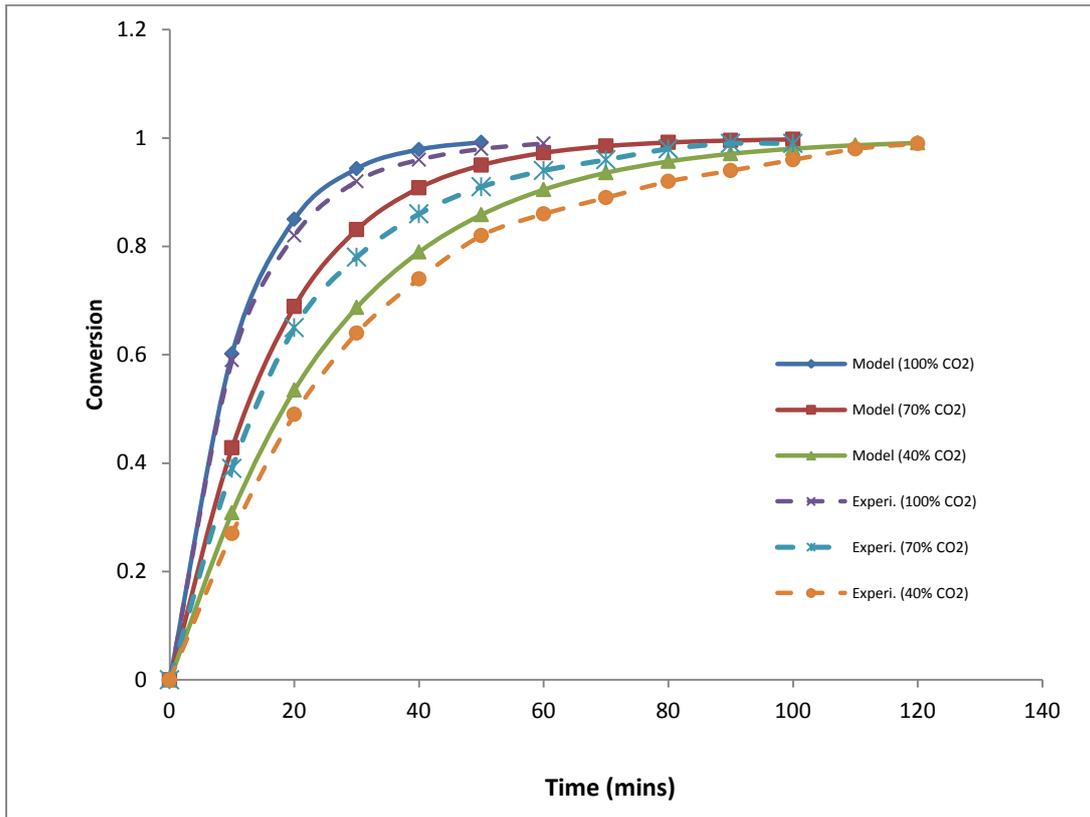


Fig. 5. Graphical result of Udi char gasification at 1000°C for different CO<sub>2</sub> Concentrations

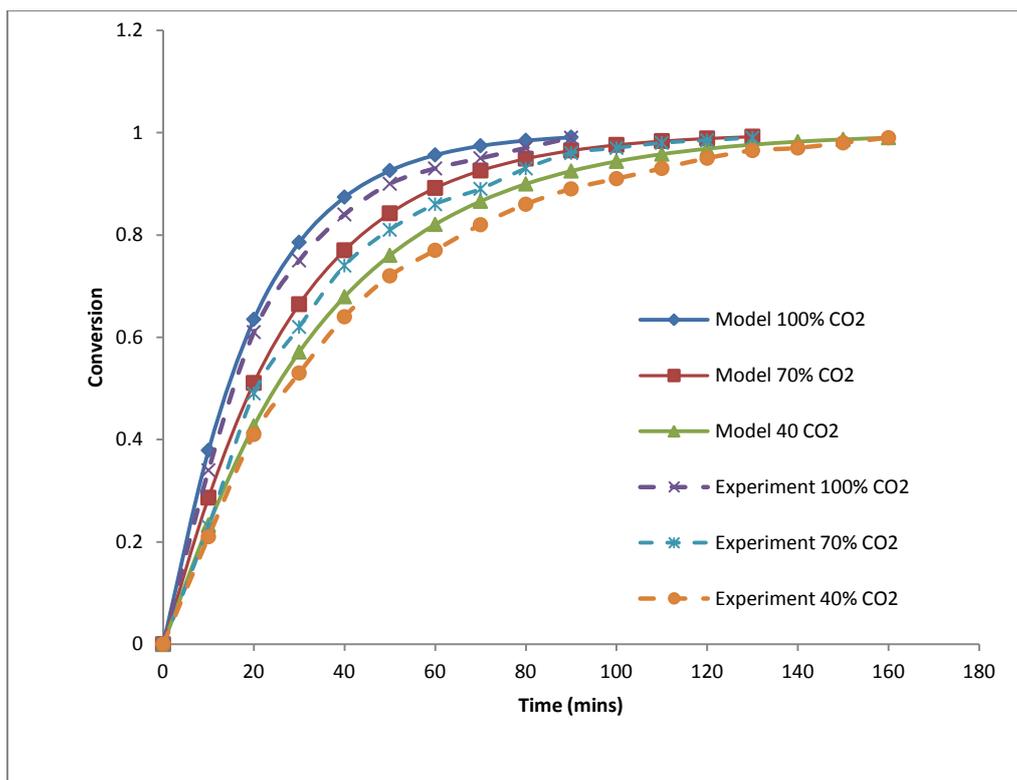


Fig. 6. Graphical result of Udi char gasification at 950°C different CO<sub>2</sub> concentrations

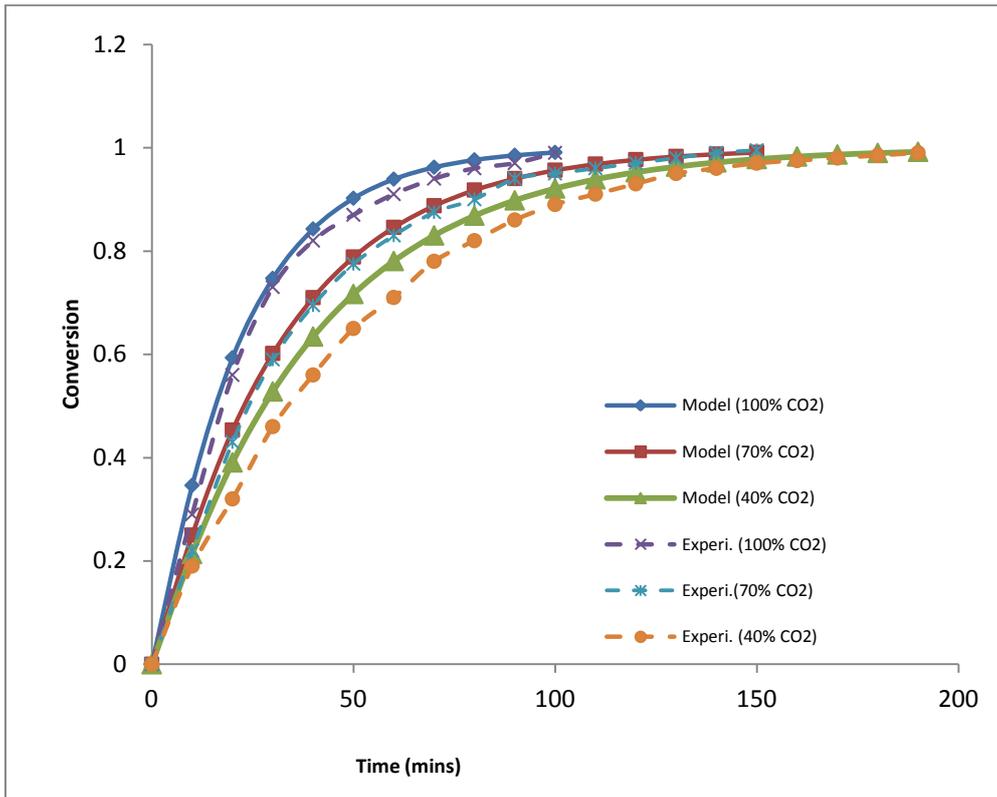


Fig. 7. Graphical result of Udi char gasification at 900°C for different CO<sub>2</sub> Concentrations

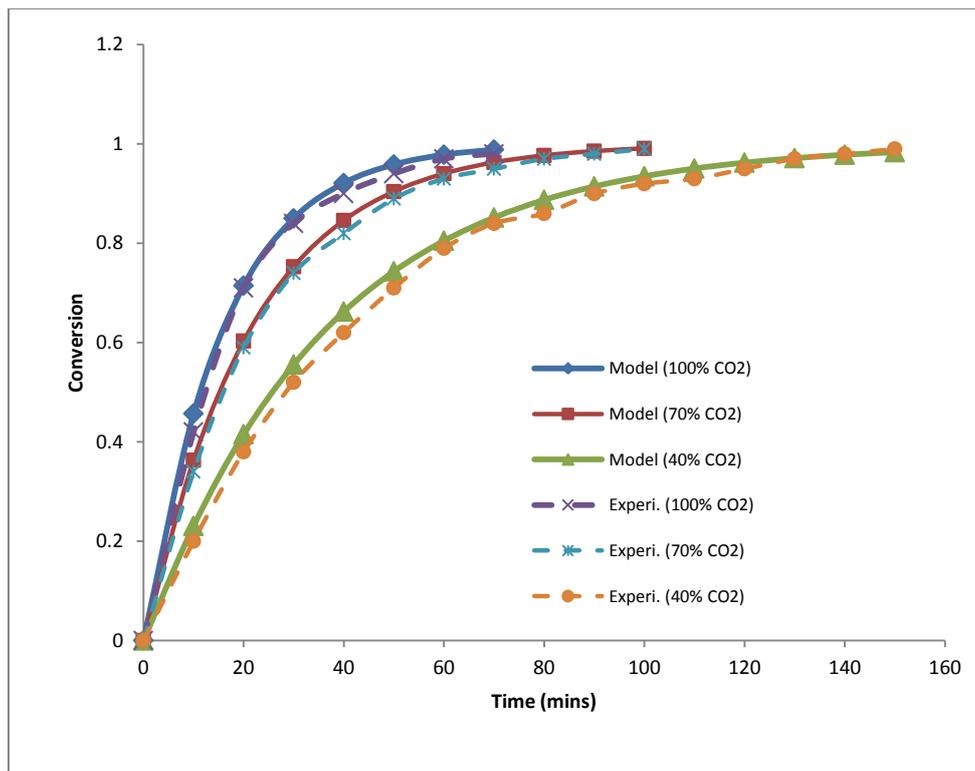


Fig. 8. Graphical Result of Okaba char gasification at 1000°C for different CO<sub>2</sub> Concentration

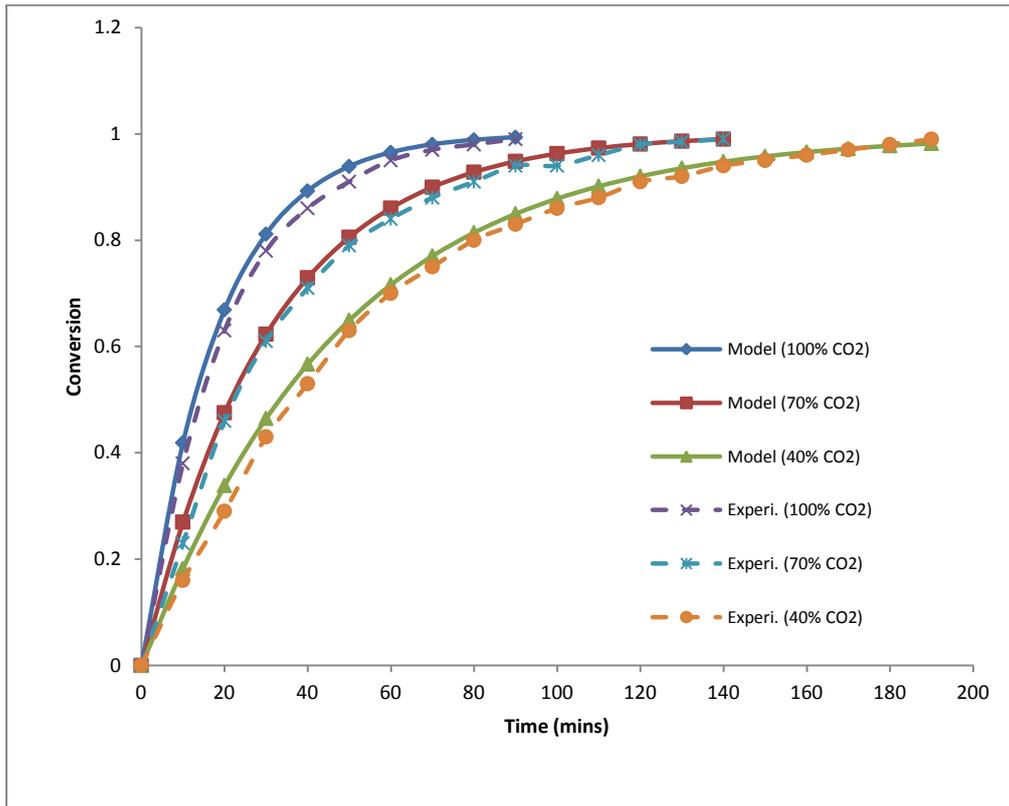


Fig. 9. Graphical result of Udi char gasification at 950°C different CO<sub>2</sub>

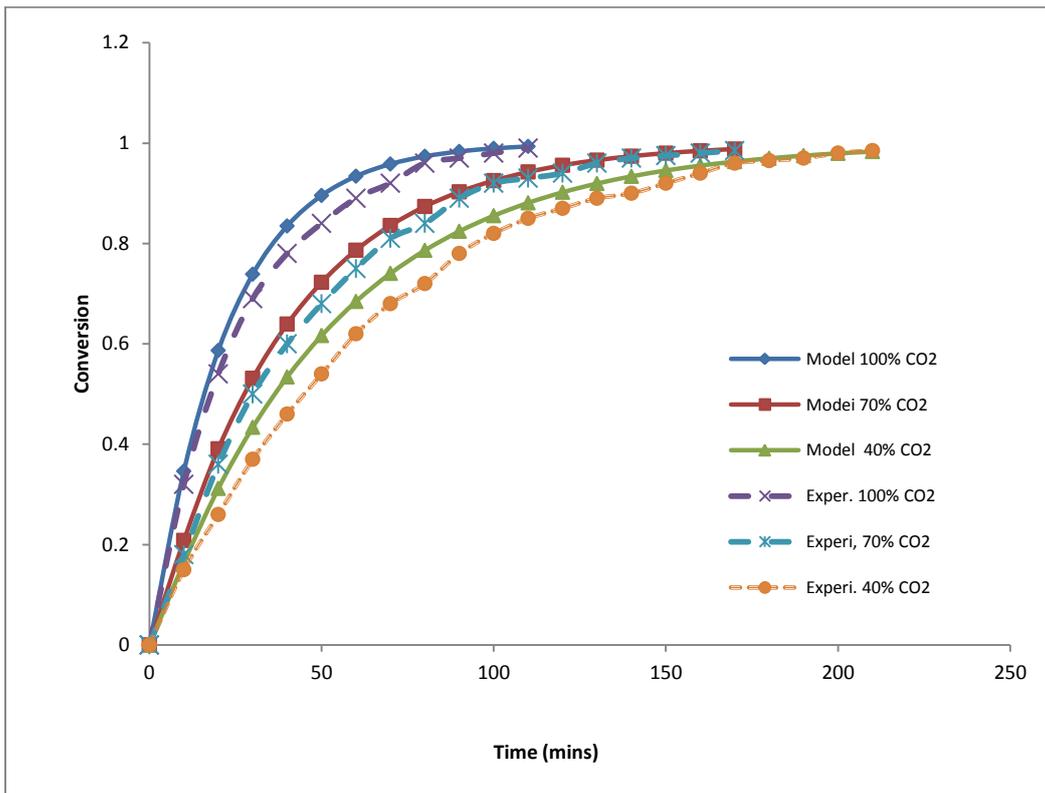


Fig. 10. Graphical result of Okaba char gasification at 950°C different CO<sub>2</sub>

#### 4. CONCLUSION

The kinetic study and modeling of Nigerian sub-bituminous coal char using the random pore technique was carried out. Proximate analysis of the coal samples shows that Udi coal has a greater heating value and poses a higher risk of spontaneous combustion than Okaba coal, as it contains more fixed carbon and volatile matter. Nonetheless, both coal samples are suitable for fuel.

The char-CO<sub>2</sub> gasification is an endothermic reaction since heat has to be supplied at relatively slow rate and the single product evolved is carbon monoxide, which renders the analysis simple and reliable.

The reactivity of char gasification and increase of pyrolysis heating rate is due to the development of active surface area at higher pyrolysis heating rates, and also due to increase of the surface area during the course of gasification [19].

Based on the results obtained from both coal samples, it was observed that concentration of the gasifying gas (carbon dioxide) affected the conversion rate. A monotonically increasing specific rate of conversion with time was observed in both cases. As the reaction temperature and concentration of the gasifying gas increases, the rate of conversion also increases, but the time required for complete conversion decreases.

#### COMPETING INTERESTS

Authors have declared that no competing interests exist.

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